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Y—115—2019

FACULTY OF SCIENCE

B.Sc. (Second Year) (Fourth Semester) (Backlog) EXAMINATION

OCTOBER/NOVEMBER, 2019

MATHEMATICS

(Partial Differential Equation-XI)

(MCQ + Theory)

(Friday, 20-12-2019)

Time : 2.00 p.m. to 4.00 p.m.

Time— Two Hours

Maximum Marks—40

N.B. :— (i) All questions are compulsory.

(ii) Use only black ball point pen for first question.

(iii) Darken only one circle for most correct answer of each MCQ.

(iv) Negative marking system is applicable for first question.

(MCQ)

1. Choose most *correct* answer of the following : 1 each

(i) Partial differential coefficientis denoted by 's'

(a) $\frac{\partial^2 z}{\partial x^2}$

(b) $\frac{\partial^2 z}{\partial y^2}$

(c) $\frac{\partial^2 z}{\partial x \partial y}$

(d) $\frac{\partial z}{\partial y}$

(ii) From the partial differential equation of the function :

$$z = f(x^2 - y^2)$$

(a) $xq + yp = 0$

(b) $xq - yp = 0$

(c) $xp - yq = 0$

(d) $xp + yq = 0$

(iii) In the method of multipliers l, m, n are chosen in such a way that :

(a) $lP + mQ + nR > 0$

(b) $lP + mQ + nR = 0$

(c) $lP + mQ + nR < 0$

(d) None of these

P.T.O.

(iv) In partial differential equation, the equation of type $f(z, p, q) = 0$, then equation requires :

- (a) Not containing x and y (b) containing x only
(c) containing y only (d) containing x and y .

(v) An equation of type

$$a_0 \frac{\partial^n z}{\partial x^n} + a_1 \frac{\partial^n z}{\partial x^{n-1} \partial y} + \dots + a_n \frac{\partial^n z}{\partial y^n} = F(x, y)$$

is called

- (a) Partial differential equation with constant coefficient.
(b) n th order partial differential equation.
(c) Homogeneous linear partial differential equation.
(d) All of the above

(vi) The complementary function of $2 \frac{\partial^2 z}{\partial x^2} + 5 \frac{\partial^2 z}{\partial x \partial y} + 2 \frac{\partial^2 z}{\partial y^2} = 0$ is :

- (a) $z = f_1(2y - x) + f_2(y - 2x)$ (b) $z = f_1(y + 2x) + f_2(y - 2x)$
(c) $z = f_1(y - 2x) + f_1(x + y)$ (d) $z = f_1(y + \frac{1}{2}x) + f_1(y - 2x)$

(vii) Order of a partial differential equation is as that of the order differential coefficient into it.

- (a) same (b) greater than
(c) less than (d) all of the above

(viii) The particular integral of partial differential equation $f(D, D') = \sin(ax + by)$ is :

- (a) $\frac{\sin(ax + by)}{f(-a^2, -ab, b^2)}$ (b) $\frac{\sin(ax + by)}{f(-a^2, -ab, -b^2)}$
(c) $\frac{\cos(ax + by)}{f(-a^2, -ab, b^2)}$ (d) $\frac{\cos(ax + by)}{f(a^2, ab, b^2)}$

- (ix) The equation of type $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0$ is called :
- Radio equation
 - Wave equation
 - Two-dimensional heat flow equation
 - One-dimensional heat flow equation
- (x) The solution of wave equation is obtained by usingmethod.
- D'Almbert's
 - Lagrange's
 - Charpit's
 - Euler's

(Theory)

2. Attempt any *two* of the following : 5 each

- (a) Form a partial differential equation from :

$$x^2 + y^2 = (z - c)^2 \tan^2 \alpha$$

- (b) Explain in detail the method of solving Lagrange's equation.
 (c) Solve :

$$(x^2 - yz)p + (y^2 - zx)q = z^2 - xy$$

where $p = \frac{\partial z}{\partial x}$ and $q = \frac{\partial z}{\partial y}$.

3. Attempt any *two* of the following : 5 each

- (a) Explain the rules for finding the particular integral of partial differential equation :

$$f(D, D) = F(x, y)$$

when :

- $F(x, y) = e^{ax+by}$
- $F(x, y) = \cos(ax + by)$.

P.T.O.

(b) Solve :

$$p^2 - q^2 = 1$$

where $p = \frac{\partial z}{\partial x}$ and $q = \frac{\partial z}{\partial y}$.

(c) Find the general integral of the equation :

$$\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial y^2} = x - y$$

4. Attempt any *two* of the following :

5 each

(a) Solve the wave equation :

$$\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial x^2}$$

by D'Alembert's method.

(b) Use the method of separation of variables to solve equation :

$$\frac{\partial^2 v}{\partial x^2} = \frac{\partial v}{\partial t}$$

given that $v = 0$ when $t \rightarrow \infty$, as well as $v = 0$ as $x = 0$ and $x = l$.

(c) Solve :

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} = 0 \text{ which satisfies the conditions :}$$

$$u(0, y) = u(l, y) = u(x, 0) = 0 \text{ and } u(x, a) = \sin \frac{n\pi x}{l}.$$