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NEPNY—16—2023

FACULTY OF SCIENCE

M.Sc. (NEP) (First Semester) EXAMINATION

NOVEMBER/DECEMBER, 2023

PHYSICS

Paper SPHYC-401

(Mathematical Methods in Physics)

(Wednesday, 20-12-2023)

Time : 10.00 a.m. to 1.00 p.m.

Time—Three Hours

Maximum Marks—80

- N.B. :-*
- (i) All questions carry equal marks.
 - (ii) Question No. **1** is compulsory.
 - (iii) Solve any *three* of the remaining *five* questions (Q. No. **2** to Q. No. **6**).
 - (iv) Figures to the right indicate full marks.

1. Solve the following questions : 20
- (a) Rotation of a matrix
 - (b) Generating function of Bessel polynomial
 - (c) Fourier sine and cosine transform
 - (d) Cauchy residue theorem.

P.T.O.

2. (a) Find the eigen values, eigen vectors and diagonal matrix of the following :

$$A = \begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 6 \\ 0 & 0 & 5 \end{bmatrix}$$

- (b) Discuss Gram-schmidt's orthogonalization process in detail. 20
3. (a) Obtain the Rodrigue's formula of Legendre polynomial and find the values of :

$$P_0(x), P_1(x), P_2(x) \text{ and } P_3(x)$$

- (b) Find the solution of Hermite polynomial i.e. :
 $y'' - 2xy' + 2ny = 0.$ 20

4. (a) Define what is the Laplace transform and find the Laplace transform of.

(i) $f(t) = 1$

(ii) $f(t) = \sin at$

(iii) $f(t) = \cos at$

(iv) $f(t) = \sin hat$

(v) $f(t) = \cosh at$

- (b) Explain the first and second shifting properties of Laplace transform and find the solution of differential equation using Laplace transform : 20

$$y'' + 25y = 10 \cos 5t,$$

where $y(0) = 2, y'(0) = 0.$

5. (a) Define analytic function and show that if $f(z)$ is analytic in and on the closed curve 'c' and if 'a' is any point on 'c', then :

$$f(a) = \frac{1}{2\pi i} \int_c \frac{f(z)}{z-a} dz.$$

- (b) Evaluate $\int_c (x+y)dx + x^2 y dy$:

(i) Along $y = x^2$ having (0,0) and (3,9) as end points

(ii) Along $y = 3x$ between (0,0) and (3,9).

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6. Write short notes on the following :

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- (a) Linear dependence and independence of vectors
(b) Rodrigue's formula of Laguerre's polynomial
(c) Properties and applications of Fourier series
(d) Singularities of an analytic function.