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Mathematics

B.Sc.F.Y. Sem - II

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Page No.:
Date:

Paper - IV: Geometry

Unit - I

1) Let α, β, γ be the angles which any line makes with the positive directions of the Co-ordinate axes then $\cos \alpha, \cos \beta, \cos \gamma$ are called _____ of the given line.

- a) direction Cosines b) direction ratios
 c) both a & b d) None of a) & b)

2) The direction Cosines of x-axis are

- a) $(1, 0, 1)$ b) $(1, 0, 0)$ c) $(0, 1, 0)$ d) $(0, 0, 1)$

3) The direction Cosines of y-axis are

- a) $(1, 0, 1)$ b) $(1, 0, 0)$ c) $(0, 1, 0)$ d) $(0, 0, 1)$

4) The direction Cosines of z-axis are

- a) $(1, 0, 1)$ b) $(1, 0, 0)$ c) $(0, 1, 0)$ d) $(0, 0, 1)$

5) If l, m, n are d.c's of a line then

a) $l^2 + m^2 + n^2 = 0$ b) $l^2 + m^2 + n^2 = 1$

c) $l + m + n = 0$ d) $l + m + n = 1$

6) If α, β, γ are the angles which a half ray makes with the positive directions of the axes then $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$ _____

- a) 1 b) 0 c) 2 d) 3

19) Set of three numbers which are proportional to the direction Cosines of a line are called _____.

- a) direction ratios b) direction numbers
 c) both a) & b) d) none of a) & b)

2) Q) If a, b, c are the direction ratios of a line then its direction Cosines are given by:

a) $\pm \frac{a}{\sqrt{\Sigma a^2}}, \pm \frac{b}{\sqrt{\Sigma a^2}}, \pm \frac{c}{\sqrt{\Sigma a^2}}$

b) $\pm \frac{a}{\sqrt{b^2+c^2}}, \pm \frac{b}{\sqrt{a^2+c^2}}, \pm \frac{c}{\sqrt{a^2+b^2}}$

- c) both a) & b)
 d) none of a) & b)

9) If AB is any segment XX' is a line and θ is the angle between them then the projection of AB on XX' is

- a) $AB \sin \theta$ b) $AB \cos \theta$ c) $AB \tan \theta$ d) $AB \cot \theta$

10) The d.c's of the line joining the two points

$P(x_1, y_1, z_1)$ and $Q(x_2, y_2, z_2)$ is given by

a) $\frac{x_2-x_1}{l} = \frac{y_2-y_1}{m} = \frac{z_2-z_1}{n} = PQ$

b) $\frac{x_2-x_1}{l} = \frac{y_2-y_1}{m} = \frac{z_2-z_1}{n} = -PQ$

- c) both a) & b) d) none of a) & b)

⑪ The projection of the segment joining the points $P(x_1, y_1, z_1)$ & $Q(x_2, y_2, z_2)$ on a line with direction Cosines l, m, n is

- a) $(x_2 + x_1)l + (y_2 + y_1)m + (z_2 + z_1)n$
 ✓ b) $(x_2 - x_1)l + (y_2 - y_1)m + (z_2 - z_1)n$
 c) $(x_2 + x_1)l + (y_2 - y_1)m + (z_2 - z_1)n$
 d) None of the above.

⑫ The angle between lines whose direction Cosines are (l_1, m_1, n_1) and (l_2, m_2, n_2) is given by

- ✓ a) $\cos \theta = l_1 l_2 + m_1 m_2 + n_1 n_2$
 b) $\sin \theta = l_1 l_2 + m_1 m_2 + n_1 n_2$
 c) $\tan \theta = l_1 l_2 + m_1 m_2 + n_1 n_2$
 d) None of these.

⑬ If direction Cosines of two lines are perpendicular proportional to a_1, b_1, c_1 and a_2, b_2, c_2 then the lines are perpendicular if

- a) $a_1 a_2 + b_1 b_2 - c_1 c_2 = 0$
 ✓ b) $a_1 a_2 + b_1 b_2 + c_1 c_2 = 0$
 c) $a_1 a_2 - b_1 b_2 + c_1 c_2 = 0$
 d) $a_1 a_2 - b_1 b_2 - c_1 c_2 = 0$

⑭ The lines with direction Cosines (l_1, m_1, n_1) and (l_2, m_2, n_2) are parallel if

- a) the lines through the origin drawn parallel to the lines coincide.
 b) the direction Cosines of the lines are the same
 c) the direction ratios of the lines are proportional.
 ✓ d) All of the above.

6

15) The equation of the plane $2x + 3y + 4z = 7$ referred to the point $(2, -3, 4)$ as origin directions of the axes remaining the same, is _____

- a) $2x + 3y + 4z + 4 = 0$ ✓ b) $2x + 3y + 11 = 0$
 c) $2x + 3y + 4z + 21 = 0$ d) $2x + 3y - 11 = 0$

16) The degree of an equation is _____ by any transformation of axes.

- a) altered ✓ b) unaltered
 c) ~~can't say~~ undetermined d) None of these.

17) If l_1, m_1, n_1 ; l_2, m_2, n_2 ; l_3, m_3, n_3 be the direction cosines of three mutually perpendicular straight lines, then

a) $\begin{vmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{vmatrix} = 1$ b) $\begin{vmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{vmatrix} = -1$

c) $\begin{vmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{vmatrix} = \pm 1$ d) $\begin{vmatrix} l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \\ l_3 & m_3 & n_3 \end{vmatrix} = 0$

18) The direction cosines of the line joining the two points (x_1, y_1, z_1) & (x_2, y_2, z_2) are

- ✓ a) $\frac{x_2 - x_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{y_2 - y_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{z_2 - z_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$
 b) $\frac{x_1 - x_2}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{y - y_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{z_2 - z_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$
 c) $\frac{x_2 - x_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{y_1 - y_2}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{z_2 - z_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$
 d) $\frac{x_2 - x_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{y_2 - y_1}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$, $\frac{z_1 - z_2}{\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}}$

(5)

MOHIT
Page No. :
Date:

19) The projection of a line on the axes are 2, 3, 6, then what is the length of the line ?

- a) 7 b) 10 c) 13 d) 3

20) A line makes angles $\alpha, \beta, \gamma, \delta$ with the four diagonals of a cube then

a) $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma + \cos^2 \delta = \frac{1}{3}$

b) $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma + \cos^2 \delta = \frac{4}{3}$

c) $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma + \cos^2 \delta = \frac{2}{3}$

d) None of these.

Unit - II

① Every equation of the first degree in x, y, z represents _____

- a) a plane b) a line in 2D
- c) both a) & b) d) none of these.

② Equation of every plane is of the first degree i.e., of the form _____

- a) $ax + by + cz + d = 0 ; a^2 + b^2 + c^2 \neq 0$
- b) $ax + by + cz + d = 0$
- c) $ax + by + c = 0$
- d) none of the above.

③ Normal form of the equation of a plane is _____

- a) $lx + my + nz = p$ b) $lx + my + nz = p^2$
- c) $lx - my - nz = p$ d) none of these.

④ _____ are the direction ratios of the normal to the plane $ax + by + cz + d = 0$.

- a) $a, b, -c$ b) a, b, c
- c) $-a, b, -c$ d) $a, -b, c$

⑤ Direction cosines of the normal to the plane $2x - 3y + 6z = 7$ are _____

- a) $\frac{-2}{7}, \frac{3}{7}, \frac{-6}{7}$ b) $\frac{2}{7}, \frac{-3}{7}, \frac{6}{7}$
- c) $\frac{-2}{7}, \frac{-3}{7}, \frac{6}{7}$ d) None of these.

6) Angle between two planes is equal to the angle between _____ to them from any point.

- a) Normals b) tangents
c) both a) & b) d) none of a) & b)

7) Angle between two planes with direction ratios a, b, c & a_1, b_1, c_1 is _____

a) $\cos \theta \left\{ \frac{aa_1 + bb_1 + cc_1}{\sqrt{\sum a^2} \cdot \sqrt{\sum a_1^2}} \right\}$

b) $\sin \theta \left\{ \frac{aa_1 + bb_1 + cc_1}{\sqrt{\sum a^2} \cdot \sqrt{\sum a_1^2}} \right\}$

c) $\tan \theta \left\{ \frac{aa_1 + bb_1 + cc_1}{\sqrt{\sum a^2} \cdot \sqrt{\sum a_1^2}} \right\}$

d) none of these.

8) Two planes $ax + by + cz + d = 0$, $a_1x + b_1y + c_1z + d_1 = 0$ will be parallel if a, b, c & a_1, b_1, c_1 are direction ratios of _____

- a) different lines & same line
b) normal c) none of these.

9) Two planes $ax + by + cz + d = 0$, $a_1x + b_1y + c_1z + d_1 = 0$ will be perpendicular if

a) $aa_1 + bb_1 + cc_1 = 0$

b) $aa_1 - bb_1 - cc_1 = 0$

c) $aa_1 + bb_1 - cc_1 = 0$

d) $aa_1 - bb_1 + cc_1 = 0$

10) Angle between the planes $2x - y + z = 6$ & $x + y + 2z = 7$ is

- a) $\pi/6$ b) $\pi/2$ c) $\pi/3$ d) π

11) Angle between the planes $3x - 4y + 5z = 0$ & $2x - y - 2z = 5$ is

- a) $\pi/6$ b) $\pi/2$ c) $\pi/3$ d) π

12) The equation of plane in terms of the intercepts a, b, c which it makes on the axes is

a) $\frac{x}{a} - \frac{y}{b} - \frac{z}{c} = 1$ b) $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$

c) $\frac{x}{a} - \frac{y}{b} + \frac{z}{c} = 1$ d) $\frac{x}{a} + \frac{y}{b} - \frac{z}{c} = 1$

13) The equation of plane through three non-collinear points (x_1, y_1, z_1) , (x_2, y_2, z_2) and (x_3, y_3, z_3) is given by

a)
$$\begin{vmatrix} x & y & z & 1 \\ x_1 & y_1 & z_1 & 1 \\ x_2 & y_2 & z_2 & 1 \\ x_3 & y_3 & z_3 & 1 \end{vmatrix} = 0$$
 b)
$$\begin{vmatrix} x & y & z & 1 \\ x_1 & y_1 & z_1 & 1 \\ x_2 & y_2 & z_2 & 1 \\ x_3 & y_3 & z_3 & 1 \end{vmatrix} = 1$$

c)
$$\begin{vmatrix} x & y & z & 1 \\ x_1 & y_1 & z_1 & 1 \\ x_2 & y_2 & z_2 & 1 \\ x_3 & y_3 & z_3 & 1 \end{vmatrix} = 2$$
 d)
$$\begin{vmatrix} x & y & z & 1 \\ x_1 & y_1 & z_1 & 1 \\ x_2 & y_2 & z_2 & 1 \\ x_3 & y_3 & z_3 & 1 \end{vmatrix} = -1$$

(9)

14) The equation of plane through the points $P(2, 2, -1)$, $Q(3, 4, 2)$, $R(7, 0, 6)$ is

a) $5x + 2y - 3z + 17 = 0$ ✓ ~~b) $5x + 2y - 3z - 17 = 0$~~
 c) $5x - 2y + 3z - 17 = 0$ d) $5x - 2y + 3z + 17 = 0$

15) If k is a parameter then the equation $ax + by + cz + k = 0$ represents the system of planes _____ to a given plane.

a) $ax + by + cz + d = 0$.

- a) perpendicular b) not perpendicular
 c) parallel d) not parallel

16) The equation _____ represents the system of planes through the line of intersection of the planes $ax + by + cz + d = 0$ and $a_1x + b_1y + c_1z + d_1 = 0$.

- a) $(ax + by + cz + d) + k(a_1x + b_1y + c_1z + d_1) = 0$
 b) $(ax + by + cz + d) \cdot (a_1x + b_1y + c_1z + d_1) = 0$
 c) both a) & b)
 d) none of a) & b)

17) The equation of the plane passing through the intersection of the planes $x + y + z = 6$ and $2x + 3y + 4z + 5 = 0$ and the point $(1, 1, 1)$ is _____.

- a) $20x + 23y + 26z + 69 = 0$
 ✓ b) $20x + 23y + 26z - 69 = 0$
 c) $20x - 23y + 26z + 69 = 0$
 d) $20x + 23y - 26z - 69 = 0$

18) Two points $A(x_1, y_1, z_1)$, $B(x_2, y_2, z_2)$ lie on the same side of the plane $ax+by+cz+d=0$ if $ax_1+by_1+cz_1+d_1$ and $ax_2+by_2+cz_2+d_2$ have

- a) different signs
- b) same signs
- c) always on the same side
- d) none of these

19) The length of the perpendicular from the point (x_1, y_1, z_1) to the plane $ax+by+cz+d=0$ is

a) $\pm \frac{ax_1+by_1+cz_1+d}{\sqrt{a^2+b^2+c^2}}$ b) $\pm \frac{ax_1-by_1+cz_1+d}{\sqrt{a^2+b^2+c^2}}$
 c) $\pm \frac{ax_1+by_1-cz_1+d}{\sqrt{a^2+b^2+c^2}}$ d) $\pm \frac{ax_1+by_1+cz_1-d}{\sqrt{a^2+b^2+c^2}}$

20) If $ax+by+cz+d=0$ & $a_1x+b_1y+c_1z+d_1=0$ are two plane then the equation of bisecting planes is

a) $\frac{ax+by+cz+d}{\sqrt{a^2+b^2+c^2}} = \frac{a_1x+b_1y+c_1z+d_1}{\sqrt{a_1^2+b_1^2+c_1^2}}$

b) $\frac{ax+by+cz+d}{\sqrt{a^2+b^2+c^2}} = -\frac{a_1x+b_1y+c_1z+d_1}{\sqrt{a_1^2+b_1^2+c_1^2}}$

c) $\frac{ax+by+cz+d}{\sqrt{a^2+b^2+c^2}} = \pm \frac{a_1x+b_1y+c_1z+d_1}{\sqrt{a_1^2+b_1^2+c_1^2}}$

d) none of these.

Unit - III

1) The equation of line passing through a given point $A(x_1, y_1, z_1)$ and having direction cosines l, m, n are is —

a) $\frac{x-x_1}{l} = \frac{y-y_1}{m} = \frac{z-z_1}{n}$

b) $\frac{x-x_1}{l^2} = \frac{y-y_1}{m^2} = \frac{z-z_1}{n^2}$

c) $\frac{x-x_1}{l} + \frac{y-y_1}{m} + \frac{z-z_1}{n} = 0$

d) none of these.

2) The equations of the line through two points (x_1, y_1, z_1) & (x_2, y_2, z_2) is

a) $\frac{x-x_1}{x_1-x_2} = \frac{y-y_1}{y_2-y_1} = \frac{z-z_1}{z_2-z_1}$

b) $\frac{x-x_1}{x_2-x_1} = \frac{y-y_1}{y_2-y_1} = \frac{z-z_1}{z_2-z_1}$

c) $\frac{x_1-x}{x_2-x_1} = \frac{y-y_1}{y_2-y_1} = \frac{z-z_1}{z_2-z_1}$

d) none of these.

3) To transform the equations $ax+by+cz+d=0$ to symmetrical form, we require,

a) the direction ratios of the line, and

b) the co-ordinates of any one point on it.

c) both a) & b) d) none of these.

4) The angle between the line and the plane (where line is given by $\frac{x-x_1}{l} = \frac{y-y_1}{m} = \frac{z-z_1}{n}$ & plane is given by $ax+by+cz+d=0$) is

a) $\cos \alpha = \frac{al+bm+cn}{\sqrt{a^2+b^2+c^2} \cdot \sqrt{l^2+m^2+n^2}}$

b) $\sin \alpha = \frac{al+bm+cn}{\sqrt{a^2+b^2+c^2} \cdot \sqrt{l^2+m^2+n^2}}$

c) $\tan \alpha = \frac{al+bm+cn}{\sqrt{a^2+b^2+c^2} \cdot \sqrt{l^2+m^2+n^2}}$

d) none of these.

5) If the straight line is parallel to the plane then

a) $al+bm+cn=0$ b) $al-bm-cn=0$

c) $al-bm+cn=0$ d) $al+bm-cn=0$

6) Conditions for the line $\frac{x-x_1}{l} = \frac{y-y_1}{m} = \frac{z-z_1}{n}$ to lie in the plane $ax+by+cz+d=0$ are

a) $al+bm+cn=0$ b) $ax_1+by_1+cz_1+d=0$

c) both a) & b) d) none of a) & b)

7) The general equation of a plane containing the line

$$\frac{x-x_1}{l} = \frac{y-y_1}{m} = \frac{z-z_1}{n} \text{ is}$$

a) $A(x-x_1) + B(y-y_1) + C(z-z_1) = 0$

b) $A(x-x_1) + B(y-y) + C(z-z_1) = 0$

c) both a) & b)

d) none of a) & b)

8) Which of the following equation represents the plane which passes through the line

$$\frac{x-x_1}{l_1} = \frac{y-y_1}{m_1} = \frac{z-z_1}{n_1} \text{ and}$$

parallel to

$$\frac{x-x_2}{l_2} = \frac{y-y_2}{m_2} = \frac{z-z_2}{n_2} \text{, ~~is given by~~}$$

a) $\begin{vmatrix} x-x_1 & y-y_1 & z-z_1 \\ l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \end{vmatrix} = 0$

b) $\begin{vmatrix} x-x_2 & y-y_2 & z-z_2 \\ l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \end{vmatrix} = 0$

~~c) both a) & b)~~

d) None of a) & b)

9) Which of the following equation represents the plane which passes through the line

$$\frac{x-x_2}{l_2} = \frac{y-y_2}{m_2} = \frac{z-z_2}{n_2} \text{ and}$$

parallel to $\frac{x-x_1}{l_1} = \frac{y-y_1}{m_1} = \frac{z-z_1}{n_1}$.

a) $\begin{vmatrix} x-x_1 & y-y_1 & z-z_1 \\ l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \end{vmatrix} = 0$

b) $\begin{vmatrix} x-x_2 & y-y_2 & z-z_2 \\ l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \end{vmatrix} = 0$

c) both a) & b)

d) none of a) & b)

10) The equation of straight line involve ~~no~~ arbitrary constants ?

- a) one
- b) two
- c) three
- d) four

11) If $u_1 = 0 = v_1$ & $u_2 = 0 = v_2$ be two straight lines, then the general equation of a straight line intersecting them both are

- a) $u_1 + \lambda v_1 = 0 = u_2 + \lambda v_2$
- b) $u_1 + \lambda v_1 = 1 = u_2 + \lambda v_2$
- c) $u_1 + \lambda v_1 = 2 = u_2 + \lambda v_2$
- d) none of these.

12) The magnitude and the equation of the line of shortest distance between the lines $\frac{x-8}{3} = \frac{y+9}{-16} = \frac{z-10}{7}$ &

$\frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}$ is

- a) 14 and $117x + 4y - 41z - 490 = 0 = 9x - 4y - z = 19$
- b) 13 and $117x - 4y + 41z + 490 = 0 = 9x - 4y - z = 4$
- c) 12 and $117x + 4y - 41z - 490 = 0 = 9x - 4y - z = 19$
- d) none of these.

13) The length of the perpendicular from a given point $P(x_1, y_1, z_1)$ to a given line

$\frac{x-\alpha}{l} = \frac{y-\beta}{m} = \frac{z-\gamma}{n}$

$PG^2 = (x_1 - \alpha)^2 + (y_1 - \beta)^2 + (z_1 - \gamma)^2$
 $- [l(x_1 - \alpha) + m(y_1 - \beta) + n(z_1 - \gamma)]^2$

14) The perpendicular distance of $P(1, 2, 3)$ from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is _____.

- a) 5 b) 6 c) 7 d) 8

15) Equation of straight line in ~~symmetrical~~ $3x + 2y - z - 4 = 0$; $6x + y - 2z + 3 = 0$ in the symmetrical form is

a) $\frac{x-2}{3} = \frac{y-5}{2} = \frac{z}{5}$ ~~$\frac{x+2}{3} = \frac{y-5}{-2} = \frac{z}{5}$~~

c) $\frac{x+2}{3} = \frac{y-5}{2} = \frac{z}{5}$ d) none of these.

16) Length of the shortest distance between the lines

$$\frac{x-3}{3} = \frac{y-8}{-1} = \frac{z-3}{+1} \quad \text{and} \quad \frac{x+3}{-3} = \frac{y+7}{2} = \frac{z-6}{4}$$

- a) $3\sqrt{30}$ b) $3/\sqrt{30}$ c) $\sqrt{30}$ d) none of these

17) The distance of the point of intersection of the line $\frac{x-3}{2} = \frac{y-4}{2} = \frac{z-5}{2}$ and

the plane $x + y + z = 17$ from the point $(3, 4, 5)$ is given by

- a) 3 b) $3\frac{1}{2}$ c) $\sqrt{3}$ d) none of these.

18) The ~~the~~ lines $\frac{x-1}{2} = \frac{y-2}{4} = \frac{z-2}{7}$
and $\frac{x-1}{4} = \frac{y-2}{5} = \frac{z-3}{7}$ are
a) parallel b) intersecting
c) skew d) perpendicular

19) The equations of the line through the point $(2, 3, -5)$ and equally inclined to the axes are

- a) $x-2 = y-3 = z+5$ b) $\frac{x-1}{2} = \frac{y-1}{3} = \frac{z+1}{-5}$
c) $\frac{x}{2} = \frac{y}{3} = \frac{z}{-5}$ d) none of them

20) The line $\frac{x-2}{3} = \frac{y-3}{4} = \frac{z-4}{5}$ is parallel to the plane

- a) $2x+y-2z=0$ b) $3x+4y+5z=7$
c) $x+y+z=2$ d) $2x+3y+4z=0$

Unit - IV

1) The radius of the sphere $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ is

~~a) $\sqrt{u^2 + v^2 + w^2 - d}$~~ b) $\sqrt{u^2 - v^2 + w^2 - d}$

c) $\sqrt{u^2 + v^2 - w^2 - d}$ d) $\sqrt{u^2 + v^2 + w^2 + d}$

2) Centre of the sphere $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ is

a) (u, v, w) ~~b) $(-u, -v, -w)$~~

c) $(u, v, -w)$ d) $(-u, v, w)$

3) Equation to a sphere on line joining (x_1, y_1, z_1) , (x_2, y_2, z_2) as diameter is

a) $(x - x_1)(x - x_2) + (y - y_1)(y - y_2) + (z - z_1)(z - z_2) = 0$

b) $(x + x_1)(x + x_2) + (y - y_1)(y - y_2) + (z - z_1)(z - z_2) = 0$

~~c) $(x - x_1)(x - x_2) + (y - y_1)(y - y_2) + (z - z_1)(z - z_2) = 0$~~

d) none of these

4) Equation ^{to the} sphere through the points $(0, 0, 0)$, $(0, 1, 7)$, $(-1, 2, 0)$, $(1, 2, 3)$ is

a) $7(x^2 + y^2 + z^2) + 15x + 25y + 11z = 0$

b) $7(x^2 + y^2 + z^2) + 15x - 25y + 11z = 0$

c) $7(x^2 + y^2 + z^2) + 15x + 25y - 11z = 0$

~~d) $7(x^2 + y^2 + z^2) - 15x - 25y - 11z = 0$~~

5) The sphere $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ will intersect the plane $lx + my + nz = p$ if and only if

✓ a) $(ul + vm + wn + p)^2 \leq (l^2 + m^2 + n^2)(u^2 + v^2 + w^2 - d)$

b) $(ul + vm + wn + p)^2 \geq (l^2 + m^2 + n^2)(u^2 + v^2 + w^2 - d)$

c) $(ul + vm + wn + p)^2 = (l^2 + m^2 + n^2)(u^2 + v^2 + w^2 - d)$

d) none of these.

6) The equations $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ and $lx + my + nz = p$ together represent a _____

a) line ✓ b) circle c) cone d) cylinder

7) The equation of the sphere through the circle $x^2 + y^2 + z^2 = 9$, $2x + 3y + 4z = 5$ and the point $(1, 2, 3)$ is

✓ a) $3(x^2 + y^2 + z^2) - 2x - 3y - 4z - 22 = 0$

b) $3(x^2 + y^2 + z^2) + 2x + 3y + 4z + 22 = 0$

c) $3(x^2 + y^2 + z^2) - 2x + 3y - 4z - 22 = 0$

d) none of these.

8) Equation of the tangent plane at any point (α, β, γ) of the sphere $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ is

a) $(\alpha + u)x + (\beta + v)y + (\gamma + w)z + (u\alpha + v\beta + w\gamma + d) = 0$

b) $(\alpha + u)x - (\beta + v)y + (\gamma + w)z + (u\alpha + v\beta + w\gamma + d) = 0$

✓ c) $(\alpha + u)x + (\beta + v)y + (\gamma + w)z + (u\alpha + v\beta + w\gamma + d) = 0$

d) none of these.

9) The pole of the plane $lx + my + nz = p$ with respect to the sphere $x^2 + y^2 + z^2 = a^2$ is

a) $\left(\frac{a^2 l}{p}, \frac{a^2 m}{p}, \frac{a^2 n}{p}\right)$ b) $\left(\frac{l}{p}, \frac{m}{p}, \frac{n}{p}\right)$

b) $\left(\frac{al}{p}, \frac{am}{p}, \frac{an}{p}\right)$ d) $\left(\frac{a}{p}, \frac{m}{p}, \frac{n}{p}\right)$

10) Two planes such that the pole of either lies on the other are called _____

- a) Symmetric planes b) normal planes
 c) Conjugate planes d) none of these.

11) The conditions for the two ~~planes~~ spheres $x^2 + y^2 + z^2 + 2u_1 x + 2v_1 y + 2w_1 z + d_1 = 0$ & $x^2 + y^2 + z^2 + 2u_2 x + 2v_2 y + 2w_2 z + d_2 = 0$ to be orthogonal is

- a) $2u_1 u_2 + 2v_1 v_2 + 2w_1 w_2 = d_1 + d_2$
 b) $2u_1 u_2 + 2v_1 v_2 + 2w_1 w_2 = d_1 - d_2$
 c) $2u_1 u_2 - 2v_1 v_2 - 2w_1 w_2 = d_1 + d_2$
 d) none of these.

12) The surface generated by a line which passes through a fixed point, and makes a constant angle with a fixed line through the fixed point is called _____

- a) cylinder b) sphere c) Right Circular Cone
 d) none of these.

13) The surface generated by a straight line which is always parallel to a fixed line and intersects a given curve is called

- a) cylinder
- b) cone
- c) sphere
- d) line

14) The equation of the cylinder whose generators intersect the conic $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0, z = 0$ and parallel to the line

$$\frac{x}{l} = \frac{y}{m} = \frac{z}{n} \text{ is}$$

$$a(nx-lz)^2 + 2h(mx-lz)(ny-mz) + b(ny-mz)^2 + 2gn(ax-lz) + 2fn(ny-mz) + cn^2 = 0$$

- a) $x^2 + y^2 + z^2 = 1$
- b) both a) & b)
- c) none of a) & b)

15) The surface generated by a line which intersects a fixed circle called the guiding circle, and is perpendicular to its plane is called

- a) cone
- b) right circular cylinder
- c) sphere
- d) none of these

16) The equation of right circular cylinder whose axis is the line

$$\frac{x-\alpha}{l} = \frac{y-\beta}{m} = \frac{z-\gamma}{n} \text{ and whose radius}$$

is r is given by

a) $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$; where a, b, c are dir's

✓ b) $(x-\alpha)^2 + (y-\beta)^2 + (z-\gamma)^2 - \frac{[l(x-\alpha) + m(y-\beta) + n(z-\gamma)]^2}{l^2 + m^2 + n^2} = r^2$

c) both a) & b) d) none of a) & b)

17) The line which generates the surface of the cylinder is called _____.

a) generator b) axis c) guiding line d) none of these.

18) Guiding curve of a right circular cylinder is _____.

a) ellipse b) ~~circle~~ circle
c) pair of straight lines d) any closed curve

19) The radius of the sphere $x^2 + y^2 + z^2 - 2x + 4y - 6z + 7 = 0$ is

a) 49 b) 5 c) -7 ✓ d) $\sqrt{7}$

20) The equation of the sphere with centre at $(2, 3, -4)$ and touching the plane $2x + 6y - 3z + 15 = 0$ is

✓ a) $x^2 + y^2 + z^2 - 4x - 6y + 8z - 20 = 0$
b) $x^2 + y^2 + z^2 + 4x - 6y - 8z - 20 = 0$
c) $x^2 + y^2 + z^2 - 4x - 6y + 8z + 20 = 0$
d) none of these.